

## LESSON 2.2

### Notes

#### GOAL

Solve one-step equations using algebra. addition and subtraction.

#### Vocabulary

**Inverse operations** are two operations that undo each other, such as addition and subtraction.

**Equivalent equations** are equations that have the same solution(s).

#### Properties of Equality

**Addition Property of Equality** Adding the same number to each side of an equation produces an equivalent equation.

**Subtraction Property of Equality** Subtracting the same number from each side of an equation produces an equivalent equation.

**Multiplication Property of Equality** Multiplying each side of an equation by the same nonzero number produces an equivalent equation.

**Division Property of Equality** Dividing each side of an equation by the same nonzero number produces an equivalent equation.

#### EXAMPLE 1

##### Solve an equation using subtraction

Solve  $x + 11 = 15$ .

**Solution**

$x + 11 = 15$	Write original equation.
$x + 11 - 11 = 15 -$ 11	Use subtraction property of equality: Subtract 11 from each side.
$x = 4$	Simplify.

The solution is 4. Check by substituting 4 for  $x$  in the original equation.

## **CHECK**

$$x + 11 = 15$$

$$4 + 11 = 15$$

$$15 = 15. \checkmark$$

Write original equation.

Substitute 4 for  $x$ .

Solution checks.

## **EXAMPLE 2**

### **Solve an equation using addition**

Solve  $x - 8 = 17$ .

**Solution**

#### **Horizontal format**

$$x - 8 = 17$$

$$x - 8 + 8 = 17 + 8$$

$$x = 25$$

Write original equation.

Add 8 to each side.

Simplify.

#### **Vertical format**

$$x - 8 = 17$$

$$\begin{array}{r} + 8 \\ + 8 \\ \hline \end{array}$$

$$x = 25$$

The solution is 25.

## **Exercises for Examples 1 and 2**

---

**Solve the equation. Check your solution.**

1.  $x + 9 = 5$

2.  $y + 2 = -5$

3.  $19 = w + 13$

4.  $8 = z - 11$

5.  $m - 3 = 7$

6.  $n - 4 = -12$

## **EXAMPLE 3**

### **Solve an equation using division**

Solve  $7x = -63$ .

$$\frac{7x}{7} = \frac{-63}{7}$$

$$x = -9$$

Write original equation.

Divide each side by 7.

Simplify.

**EXAMPLE 4****Solve an equation using multiplication**

**Solve**  $\frac{x}{12} = 4$

$$\frac{x}{12} = 4$$

Write original equation.

$$12 \cdot \frac{x}{12} = 12 \cdot 4$$

Multiply each side by 12.

$$x = 48$$

Simplify.

**EXAMPLE 5****Solve an equation by multiplying by a reciprocal**

The coefficient of  $x$  is  $\frac{3}{5}$ . The reciprocal of  $\frac{3}{5}$  is  $\frac{5}{3}$ .

$$\frac{3}{5}x = 6$$

Write original equation.

$$\frac{3}{5} \left( \frac{3}{5}x \right) = \frac{5}{3}(6)$$

Multiply each side by the reciprocal,

$$x = 10$$

Simplify.

**Exercises for Examples 3, 4, and 5**

---

**Solve the equation. Check your solution.**

7.  $-9x = -36$

8.  $7y = 21$

9.  $\frac{x}{3} = -24$

10.  $18 = \frac{y}{-2}$

11.  $-\frac{2}{5}z = 8$

12.  $16 = \frac{4}{7}m$

## *Answer Key*

### *Lesson 2.2*

#### **Study Guide**

1.  $x = -4$
2.  $y = -7$
3.  $w = 6$
4.  $z = 19$
5.  $m = 10$
6.  $n = -8$
7.  $x = 4$
8.  $y = 3$
9.  $x = -72$
10.  $y = -36$
11.  $z = -20$
12.  $m = 28$