## LESSON 2.8

## Notes

## GOAL

Write equations in function form and rewrite formulas

## Vocabulary

An equation in $x$ and $y$ is written in function form when the dependent variable $y$ is isolated on one side of the equation.

A literal equation is an equation that contains two or more variables.

## EXAMPLE 1

## Rewrite an equation in function form

Write $9 x-4 y=8$ in function form

## Solution

To write an equation in function form, MEANS solve the equation for $\boldsymbol{y}$

$$
\begin{aligned}
9 x-4 y=8 & \text { Write original equation. } \\
-4 y=8-9 x & \text { Subtract } 9 x \text { from each } \text { si } \\
y=-2+\frac{9}{4} \mathrm{x} & \begin{array}{l}
\text { Divide each side by }-4 . \\
\text { Simplify }
\end{array}
\end{aligned}
$$

The equation $y=\frac{9}{4} x-2$ is written in function form.

## EXAMPLE 2

## Solve a literal equation

The formula for the volume of a rectangular prism is $V=l w h$. Solve the formula for $l$.

## Solution

$V=l w h \quad$ Write original equation.
$\frac{v}{w h}=\frac{l w h}{w h} \quad$ Assume $w \neq 0$ and $h \neq 0$. Divide each side by $w h$.
$\frac{v}{w h}=l \quad$ Simplify.

The rewritten equation is $\frac{v}{w h}=l$.

## Exercises for Examples 1 and 2

Write the equation in function form

1. $7 x+y=12$
2. $3 y-9 x=21$
3. $5 y-2 x=15$

Solve the literal equation
4. $I=P r t$ for $P$
5. $A=\frac{1}{2}\left(b_{1}+b_{2}\right) h$ for $b_{2}$

## EXAMPLE 3

Solve and use a geometric formula
The area $A$ of a triangle is given by the formü̆la $A=\quad b h$ where $b$ is the base and $h$ is the height

a. Solve the formula for the base $b$.
b. Use the rewritten formula to find the base of the triangle shown, which has an area of 106.8 square inches.

## Solution

a. Solve the formula for $b$.

$$
\begin{array}{ll}
A=\frac{1}{2} b h & \begin{array}{l}
\text { Write original } \\
\text { formula. }
\end{array} \\
2 A=b h & \begin{array}{l}
\text { Multiply each side by } \\
2
\end{array} \\
\frac{2 A}{h}=b & \text { Divide each side by } h .
\end{array}
$$

Substitute 106.8 for A and 12 for h in the rewritten formula.

$$
\begin{aligned}
& b=\frac{2 A}{h} \quad \text { Write rewritten formula. } \\
& b=\frac{2(106.8)}{12} \\
& \begin{array}{l}
\text { Substitute } 106.8 \text { for } A \text { and } 12 \\
b=17.8 \quad
\end{array} \\
& \text { Simplify. }
\end{aligned}
$$

The base of the triangle is 17.8 inches.

## Exercises for Example 3

The surface area $S$ of a sphere is given by the formula $S=4 \pi r^{2}$ where $r$ is the radius of the sphere
6. Solve the formula for $r$.
7. Use the rewritten formula from Exercise 6 to find $r$ when $S=314$ square meters. Use 3.14 for $\pi$.

Answer Key

## Lesson 2.8

## Study Guide

1. $y=-7 x+12$
2. $y=3 x+7$
3. $y=\frac{2}{5} x+3$
4. $\frac{I}{r t}=P$
5. $\frac{2 A}{h}-b_{1}=b_{2}$
6. $r=\sqrt{\frac{S}{4 \pi}}$
7. 5 m
