LESSON 3.6
Notes

GOAL
Write and graph direct variation equations.

## Vocabulary

Two variables $x$ and $y$ show direct variation, provided $y=a x$ and $a \neq 0$.
The nonzero number $a$ is called the constant of variation, and $y$ is said to vary directly with $x$.

EXAMPLE 1

## Identify direct variation equations

Tell whether the equation represents direct variation. If so, identify the constant of variation.
a. $6 x-3 y=12$
b. $-5 x+2 y=0$

## Solution

To tell whether the equation represents direct variation, try to rewrite the equation in the form $y=a x$.

$$
\text { a. } \begin{aligned}
6 x-3 y & =12 & & \text { Write original equation. } \\
-3 y & =-6 x+12 & & \text { Subtract } 6 x \text { from each side. } \\
y & =2 x-4 & & \text { Divide each side by }-3 .
\end{aligned}
$$

Because the equation $6 x-3 y=12$ cannot be rewritten in the form $y=a x$, it does not represent direct variation.
a

$$
\text { b. } \begin{aligned}
-5 x+2 y & =0 & & \text { Write original equation. } \\
2 y & =5 x & & \text { Add } 5 x \text { to each side. } \\
y & =\frac{5}{2} x & & \text { Simplify. }
\end{aligned}
$$

Because the equation $-5 x+2 y=0$ can be rewritten in the form $y=a x$, it represents direct variation. The constant of variation is $\frac{5}{2}$

## Exercises for Example 1

Tell whether the equation represents direct variation. If so, identify the constant of variation.

1. $3 x+5 y=0$
2. $x+2 y=1$
3. $7 x-9 y=0$

## EXAMPLE 2

## Write and use a direct variation equation

The graph of a direct variation equation is shown.
a Write the direct variation equation.
b Find the value of $y$ when $x=12$.


## Solution

a Because $y$ varies directly with $x$, the equationhas the form $y=a x$. Use the fact that $y=23$ when $x=21$ to find $a$

$$
\begin{aligned}
y & =a x & & \text { Write direct variation equation. } \\
-3 & =a(-1) & & \text { Substitute. } \\
3 & =a & & \text { Solve for } a .
\end{aligned}
$$

A direct variation equation that relates $x$ and $y$ is $y=3 x$.
b When $x=12, y=3(12)=36$. The value of $y$ when $x=12$ is 36 .

## EXAMPLE 3

Use a direct variation model
The table shows the cost $C$ of purchasing tickets for a rock concert.
a Explain why C varies directly with $t$
b Write a direct variation equation $2 \$ 36$ that relates t and C .

| Number of tickets, $\boldsymbol{t}$ | Cost, $\boldsymbol{C}$ |
| :---: | :---: |
| 2 | $\$ 36$ |
| 3 | $\$ 54$ |
| 5 | $\$ 90$ |

## Solution

a To explain why $C$ varies directly with $t$, compare the ratios $\frac{C}{\mathrm{t}}$
forall data pairs $(t, C): \frac{36}{2}=\frac{54}{3}=\frac{90}{5}=18$. Because the ratios all equal $18, C$ varies directly with $t$.
b A direct variation equation is $C=18 t$.

## Exercises for Examples 2 and 3

4 The graph of a direct variation equation passes through the point $(5,-2)$. Write a direct variation equation and find the value of $y$ when $x=20$.
5 What if ? In Example 3, suppose the ticket distributor charges $\$ 5.50$ for each transaction, no matter how many tickets are purchased, and $\$ 18$ per ticket. Is it reasonable to use a direct variation model for this situation? Explain

## Answer Key

## Lesson 3.6

## Study Guide

1. yes; $\frac{3}{5}$
2. no
3. yes; $\frac{7}{9}$
4. $y=-\frac{2}{5} x,-8$
5. No, the equation cannot be written in $y=a x$ form.
